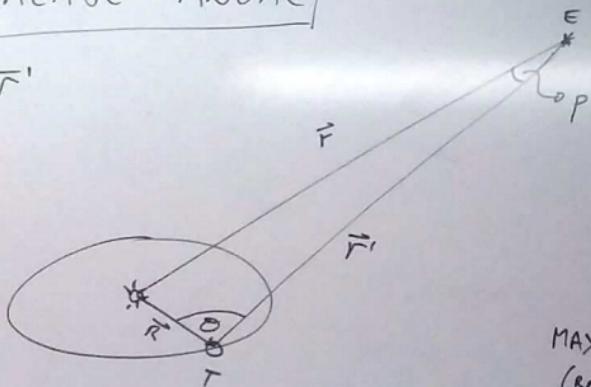
**PAR-SEC**

$$\pi = 1'' = \frac{1}{206265}$$



### PARALAJE ANUAL

$$F = \overline{R} + \overline{r}$$



1838

G1 DE CISNE

$$\frac{\text{paralaje}}{R} = \frac{\text{läng}\theta}{r}$$

$$\Rightarrow \text{paralaje} = \frac{R}{r} \cdot \text{läng}\theta$$

$$\text{MAX paralaje} = \pi = \frac{R}{r} \cdot \text{läng } 90^\circ$$

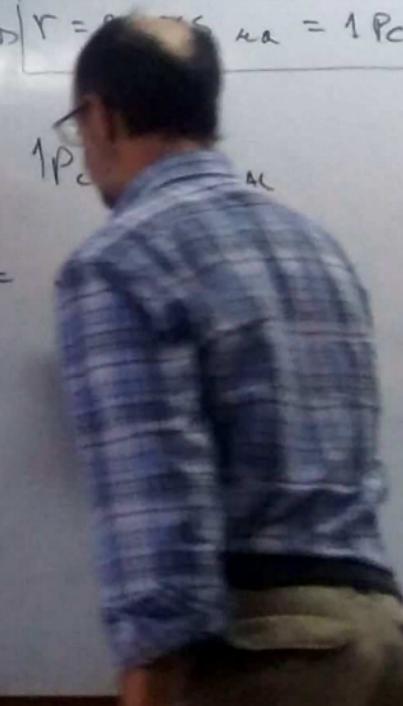
PAR-SEC

$$\pi = 1'' = \frac{1}{206265} \stackrel{\text{RAD}}{\Rightarrow} \frac{R}{r} = \frac{1 \text{ au}}{r} \Rightarrow r = 206265 \text{ au} = 1 \text{ pc}$$

1 au =  $150 \times 10^6 \text{ km}$

1 pc

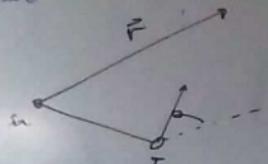
AU =



**PARALEJOS ANNUAL**

1838

G. de Cisne



$$P(\text{arcos}) = \frac{R}{r} \cdot \text{arcos}$$

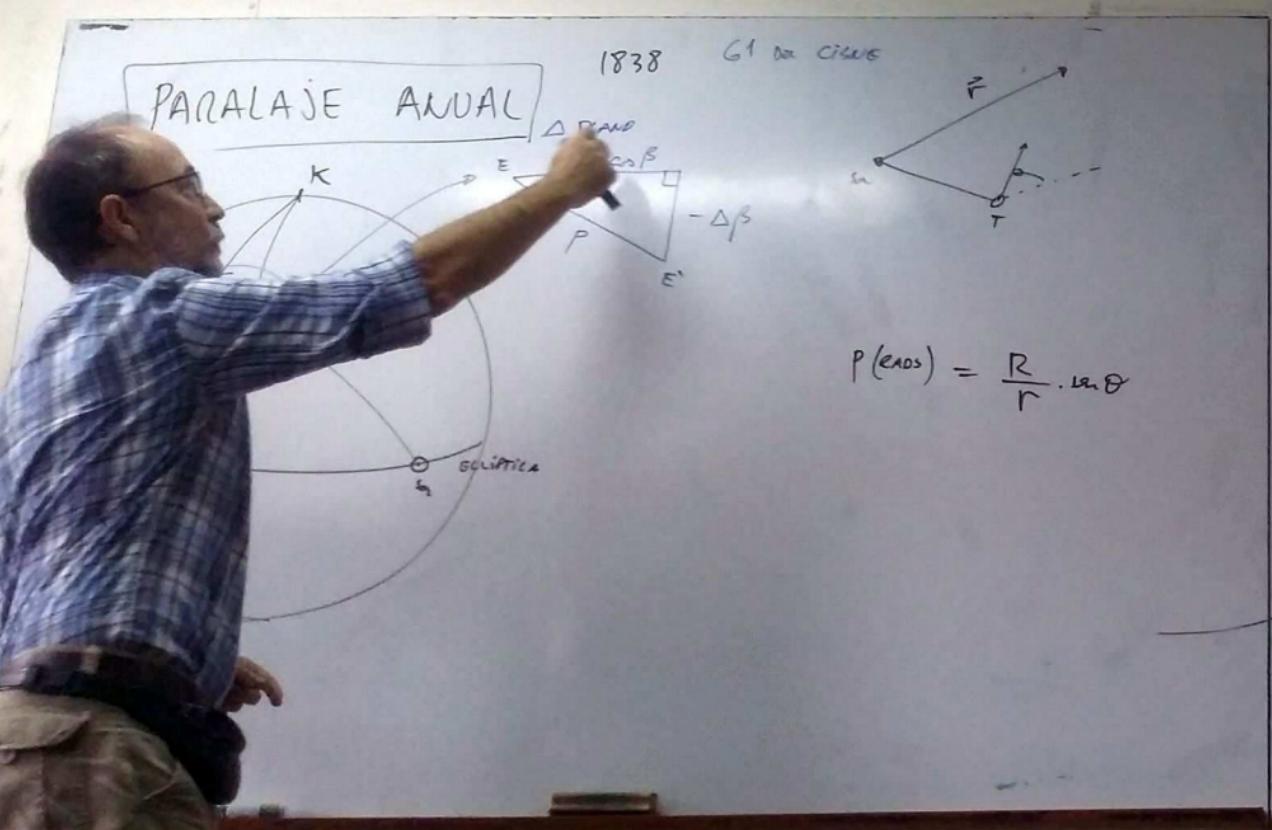
PARSEC

$$\pi = 1'' = \frac{1 \text{ arcsec}}{206265} = \frac{R}{r} = \frac{1 \text{ au}}{r} \Rightarrow r = 206265 \text{ au} = 1 \text{ pc}$$

$1 \text{ au} = 150 \times 10^6 \text{ km}$

$$1 \text{ pc} = 3,26 \text{ al}$$

$$1 \text{ al} = 300.000 \frac{\text{km}}{\text{sec}} \times 60 \times 60 \times 24 \times 365,25$$



**PAR-SEC**

$\pi = 1'' = \frac{1 \text{ rad}}{206265} = \frac{R}{r} = \frac{1 \text{ au}}{r} \Rightarrow r = 206265 \text{ au} = 1 \text{ pc}$

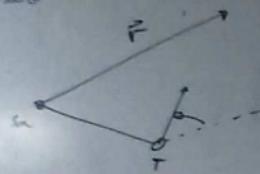
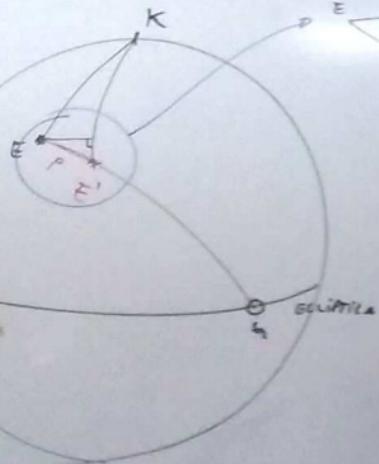
$1 \text{ pc} = 3,26 \text{ al}$

$1 \text{ al} = 300.000 \frac{\text{km}}{\text{sec}} \times 60 \times 60 \times 24 \times 365,25$

### PARALAJE ANUAL

1838

GJ DA CISSES



$$\Rightarrow \Delta\lambda \cdot \cos\beta = P \cdot \cos\gamma$$

$$-\Delta\beta = P \cdot \sin\gamma$$

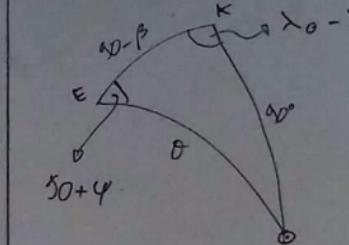
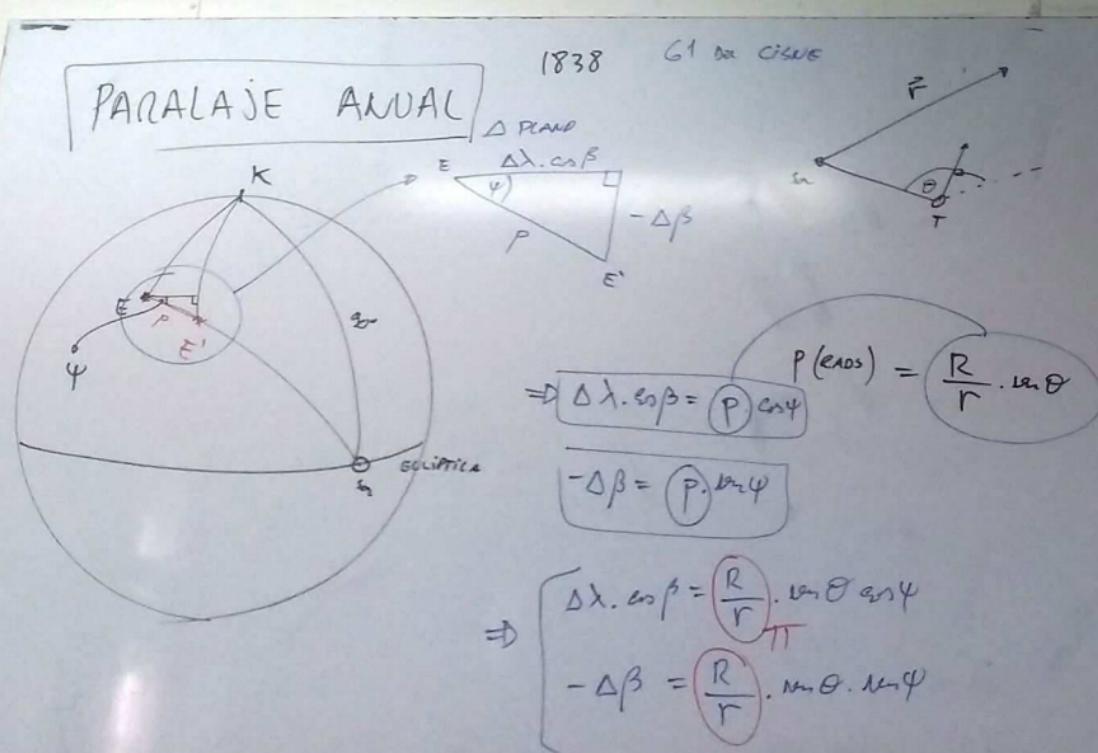
$$\Rightarrow \begin{cases} \Delta\lambda \cdot \cos\beta = \frac{R}{r} \cdot \cos\theta \cdot \cos\gamma \\ -\Delta\beta = \frac{R}{r} \cdot \sin\theta \cdot \cos\gamma \end{cases}$$

### PARSEC

$$\pi = 1'' = \frac{1 \text{ pc}}{206265} = \frac{R}{r} = \frac{1 \text{ au}}{r} \Rightarrow r = 206265 \text{ au} = 1 \text{ pc}$$

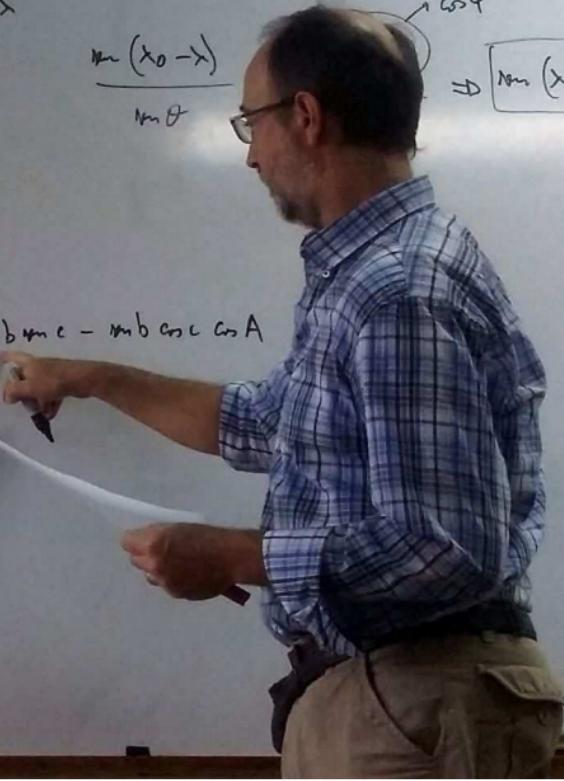
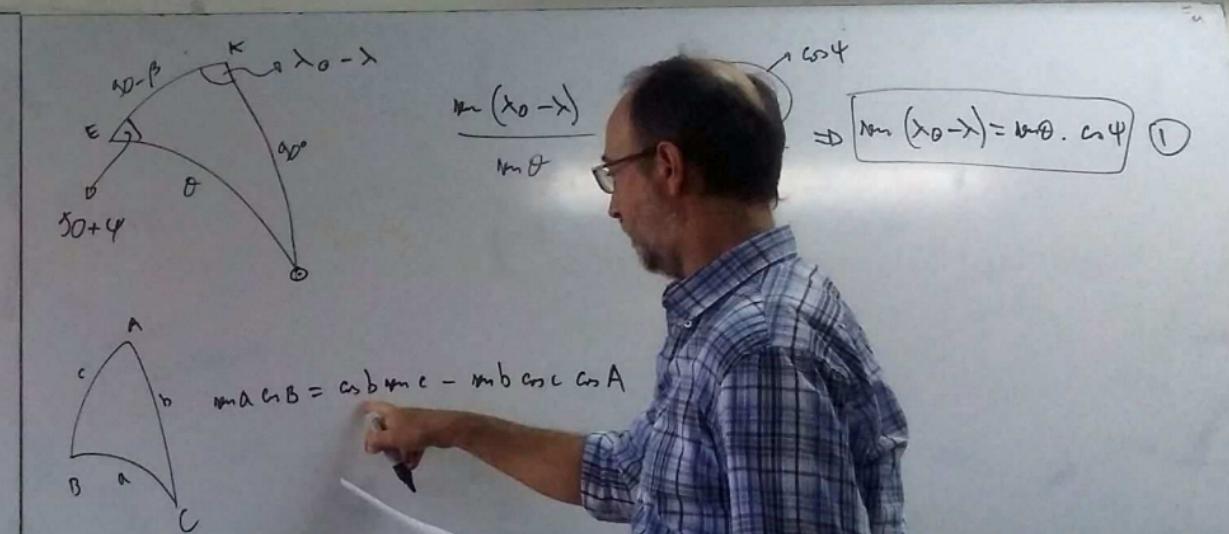
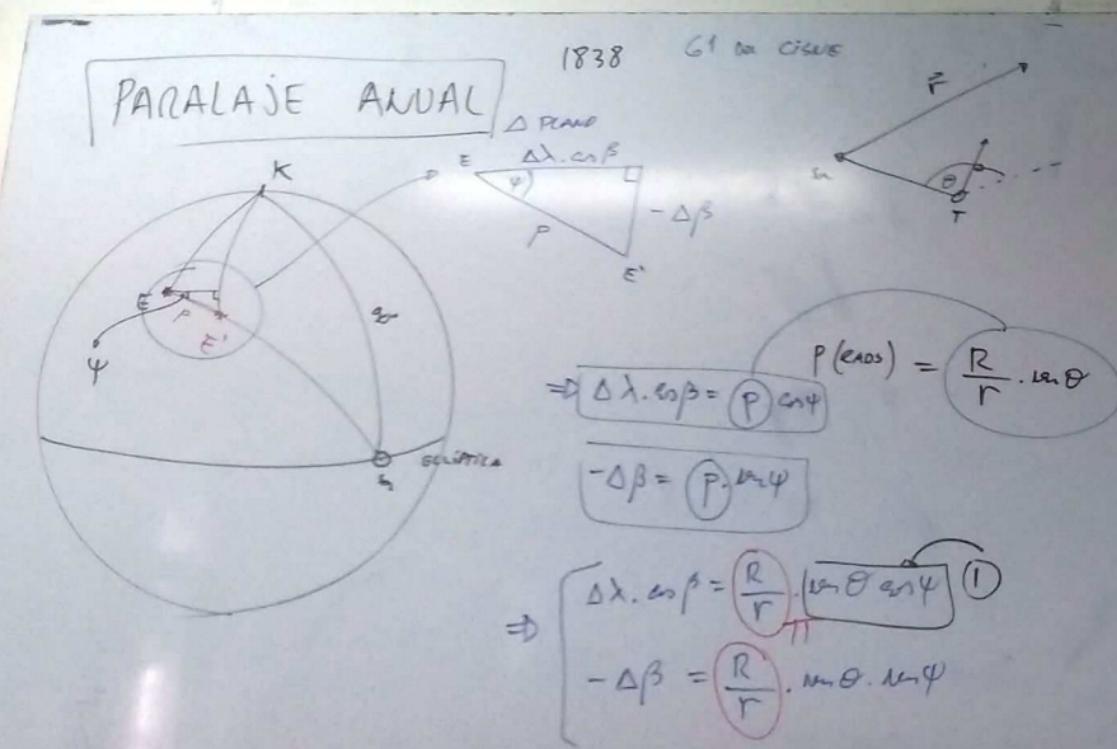
$$1 \text{ pc} = 3,26 \text{ AL}$$

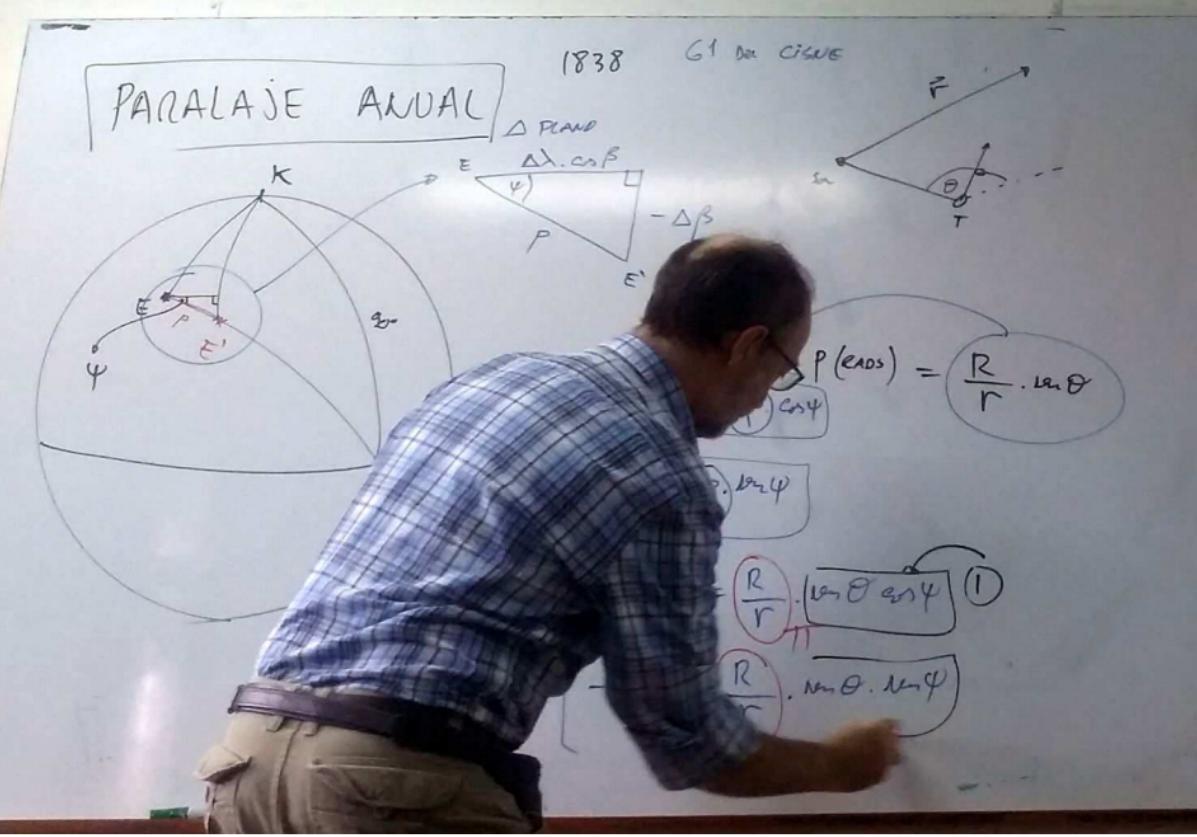
$$1 \text{ AL} = 300.000 \frac{\text{km}}{\text{sec}} \times 60 \cdot 60 \cdot 24 \cdot 365,25$$



$$\frac{\tan(\lambda_0 - \lambda)}{\tan\theta} = \frac{\tan(\lambda_0 + \lambda)}{\tan\theta}$$







$$\frac{\sin(\lambda_0 - \lambda)}{\sin \theta} = \frac{\sin(\beta + \psi)}{\sin \theta} \Rightarrow \sin(\lambda_0 - \lambda) = \sin \theta \cdot \sin \psi \quad (1)$$

$$\sin \theta \cdot \cos(\beta + \psi) = 0 - 1 \cdot \cos(\beta - \psi) \cdot \cos(\lambda_0 - \lambda)$$

$$\sin \theta \cdot (-\sin \psi) = -\sin \beta \cdot \cos(\lambda_0 - \lambda)$$

$$\sin \theta \cdot \sin \psi = \sin \beta \cdot \cos(\lambda_0 - \lambda) \quad (2)$$

PARALEAJE ANUAL

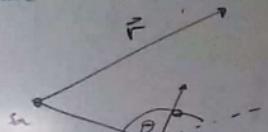
$$\Delta\lambda \cdot \cos\beta = \pi \cdot \operatorname{m}(\lambda_0 \rightarrow)$$

$$\Delta\beta = -\pi \cdot \operatorname{m}\beta \cdot \cos(\lambda_0 - \lambda)$$

$\omega(*)$

1838

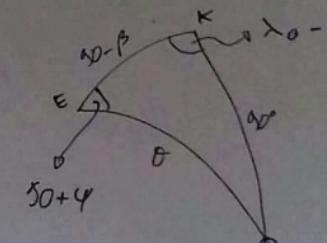
G1 da círculo



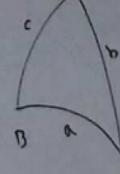
$$\Rightarrow \Delta\lambda \cdot \cos\beta = P \cdot \cos\psi \quad P(\text{exos}) = \frac{R}{r} \cdot \operatorname{m}\theta$$

$$\Delta\beta = P \cdot \sin\psi$$

$$\Rightarrow \begin{cases} \Delta\lambda \cdot \cos\beta = \frac{R}{r} \cdot (\operatorname{m}\theta \cdot \cos\psi) & (1) \\ -\Delta\beta = \frac{R}{r} \cdot [\operatorname{m}\theta \cdot \operatorname{m}\psi] & (2) \end{cases}$$



F. ANALOGA



$$\operatorname{m}A \operatorname{m}B = \operatorname{m}B \operatorname{m}C - \operatorname{m}B \operatorname{m}A \operatorname{m}C A$$

$$\operatorname{m}\theta \cdot \cos(\beta + \psi) = 0 - 1 \cdot \cos(\theta - \beta) \cdot \cos(\lambda_0 - \lambda)$$

$$\operatorname{m}\theta \cdot (-\operatorname{m}\psi) = -\operatorname{m}\beta \cdot \cos(\lambda_0 - \lambda)$$

$$\operatorname{m}\theta \operatorname{m}\psi = \operatorname{m}\beta \cdot \cos(\lambda_0 - \lambda) \quad (2)$$

F. SENO

$$\frac{\operatorname{m}(\lambda_0 - \lambda)}{\operatorname{m}\theta} = \frac{\operatorname{m}(\beta + \psi)}{\operatorname{m}\theta} \xrightarrow{\text{cos}\psi} \Rightarrow \operatorname{m}(\lambda_0 - \lambda) = \operatorname{m}\theta \cdot \cos\psi \quad (1)$$

**PARALAJE ANUAL**

$\Delta\lambda \cdot \cos\beta = \pi \cdot m \sin$

$y \Delta\beta = -\pi \cdot m \beta -$

$\lambda_0(\star)$

1838 G1 de CISE

ELÍPSE PARALÁCTICA

$$\frac{x^2}{\pi^2} + \frac{y^2}{\pi^2 \sin^2 \beta} = 1$$

$\pi \quad \pi \quad \pi \quad \pi$

ESTRUCTURA  $m \beta = \pm 90^\circ$

F. SEND

$$\frac{m(\lambda_0 - \lambda)}{m\theta} = \frac{m(90 + \psi)}{m90^\circ} \xrightarrow{\text{cos } 45^\circ} m(\lambda_0 - \lambda) = m\theta \cdot \cos \psi \quad (1)$$

F. ANALÓG

$m \alpha \sin \beta = \cos b \sin c - \sin b \cos c \cos A$

$m\theta \cdot \cos(90 + \psi) = 0 - 1 \cdot \cos(90 - \beta) \cdot \cos(\lambda_0 - \lambda)$

$m\theta \cdot (-\sin \psi) = -\sin \beta \cdot \cos(\lambda_0 - \lambda)$

$m\theta \cdot \sin \psi = \sin \beta \cdot \cos(\lambda_0 - \lambda) \quad (2)$

### PARALAJE ANUAL

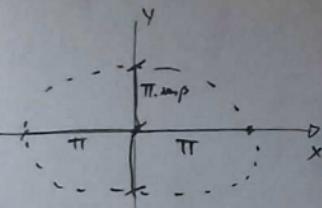
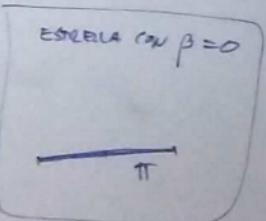
$$\Delta\lambda \cdot \cos\beta = \pi \cdot m(\lambda_0 - \lambda)$$

$$y \cdot \sin\beta = -\pi \cdot m\beta \cdot \cos(\lambda_0 - \lambda)$$

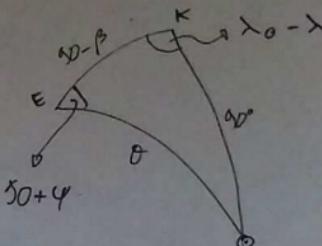
1838 G1 DA CISNE

ELÍPSE PARALÁCTICA

$$\frac{x^2}{\pi^2} + \frac{y^2}{\pi^2 m \beta} = 1$$

ESTRELLA CON  $\beta = \pm 90^\circ$ 

$\lambda_0 - \lambda$   
 $\alpha - \beta$



F. ANALÓGICA

$$m_A \sin B = \cos b \sin c - \sin b \cos c \cos A$$

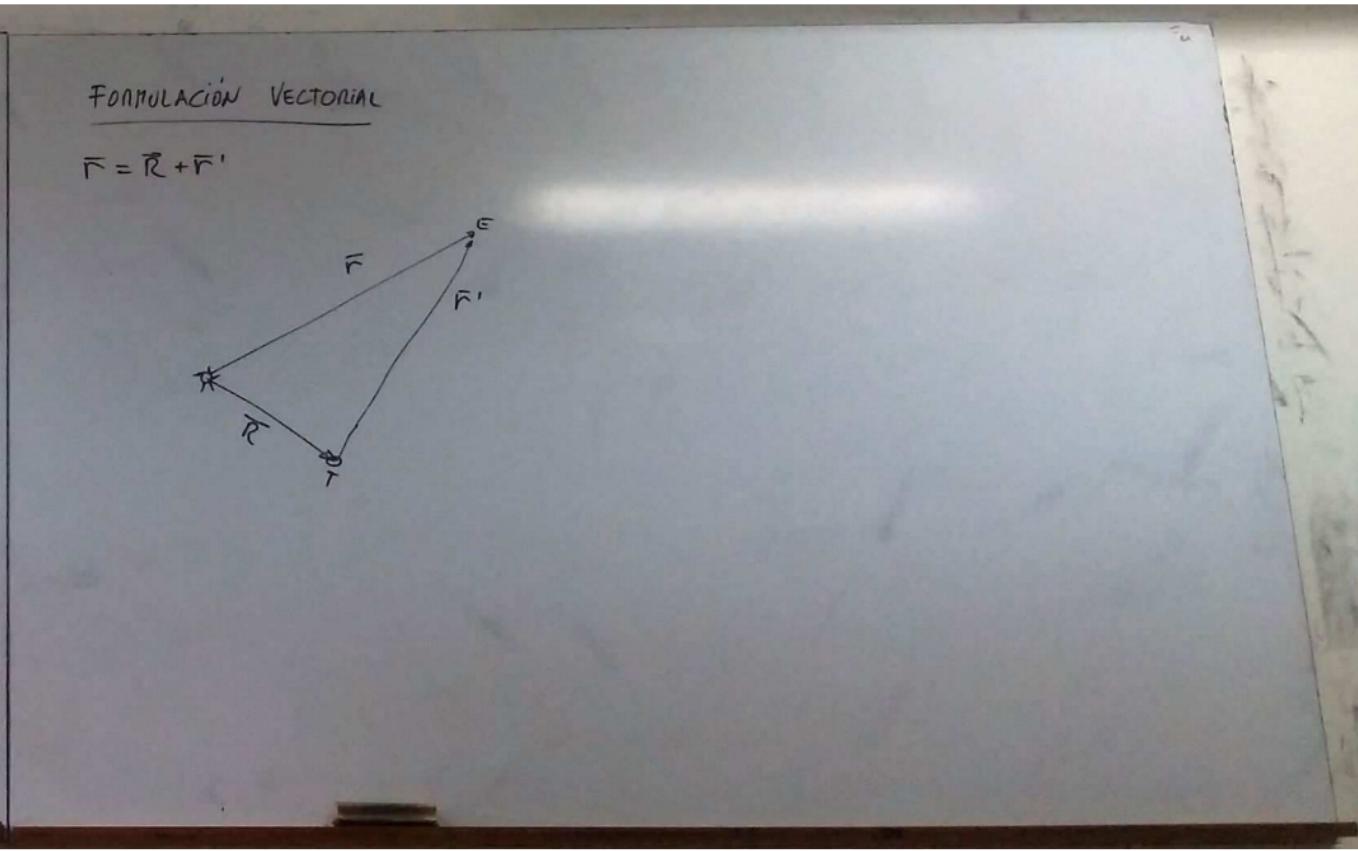
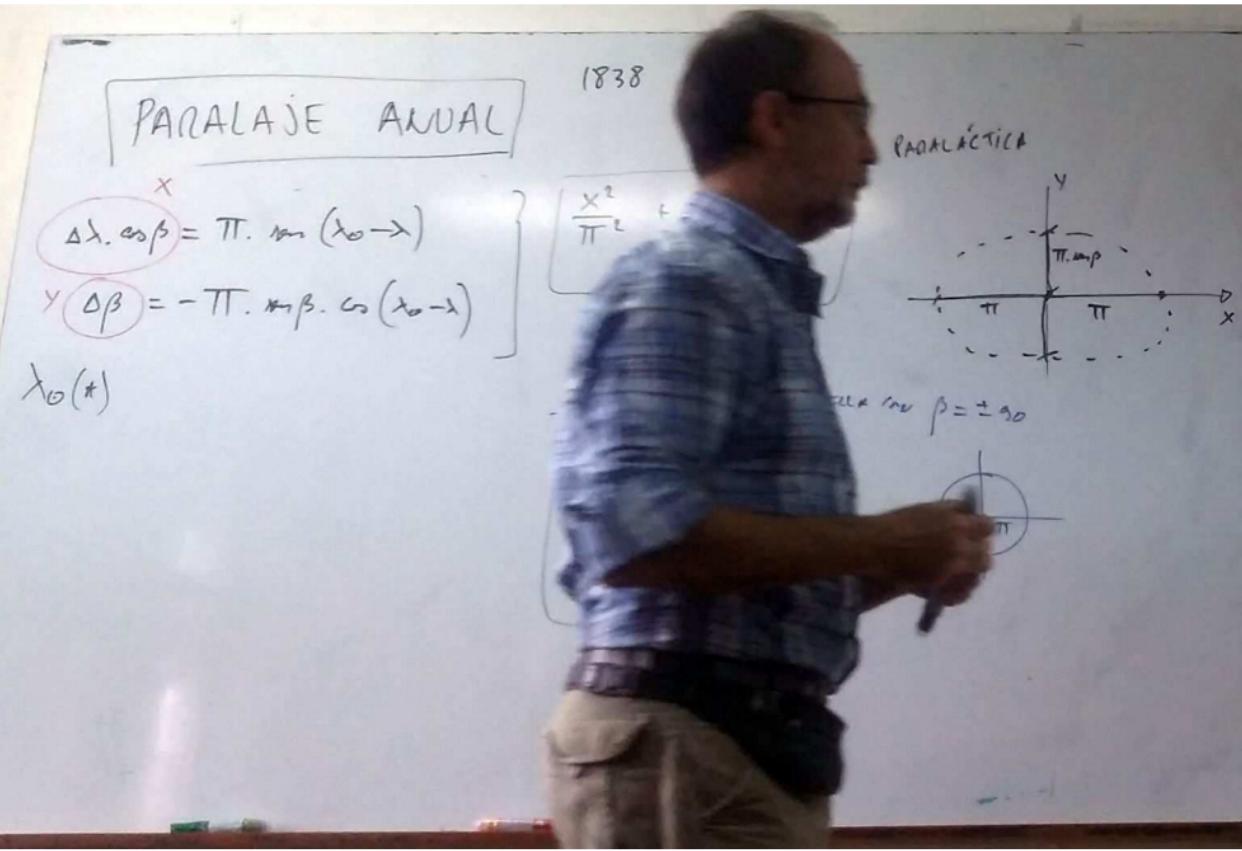
$$m\theta \cdot \cos(\alpha + \psi) = 0 - 1 \cdot \cos(\alpha - \beta) \cdot \cos(\lambda_0 - \lambda)$$

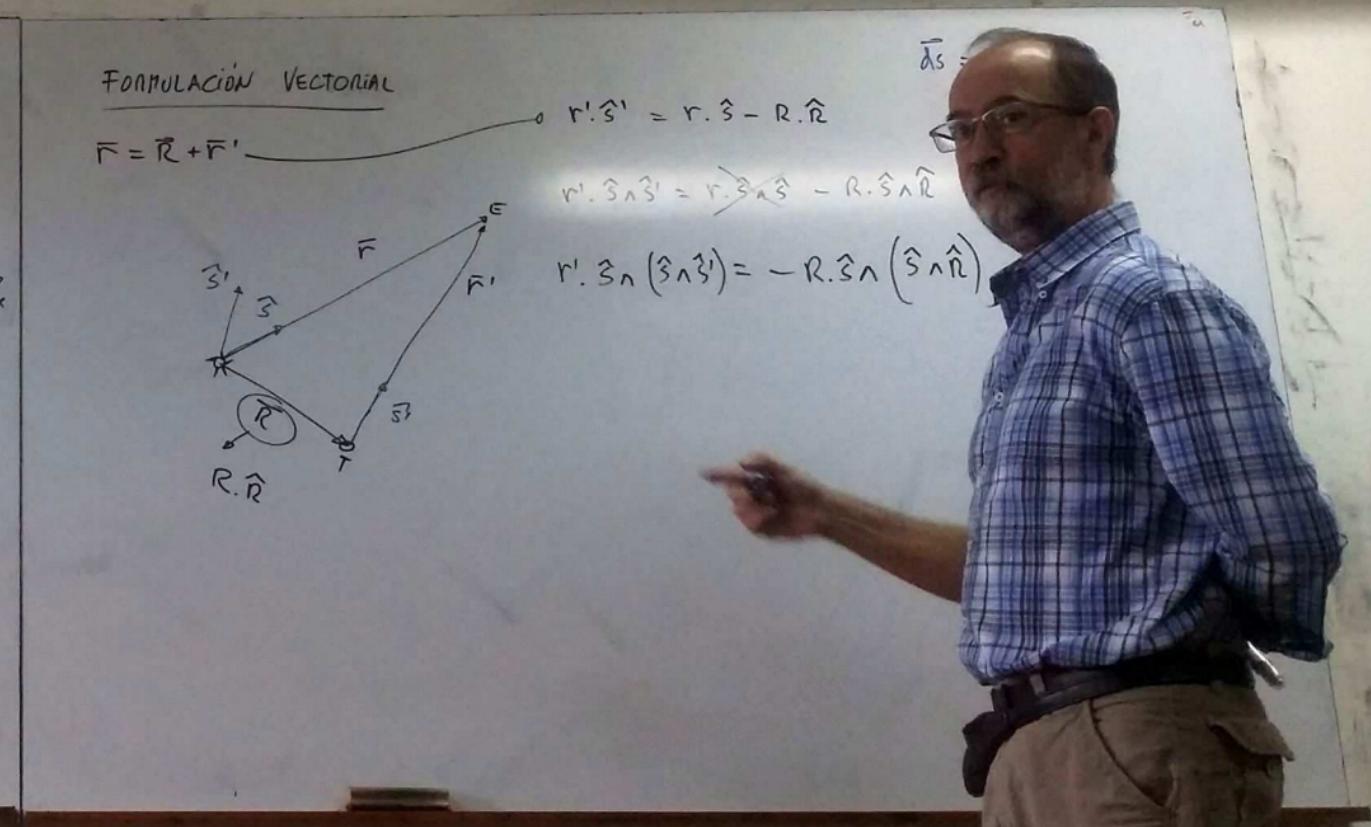
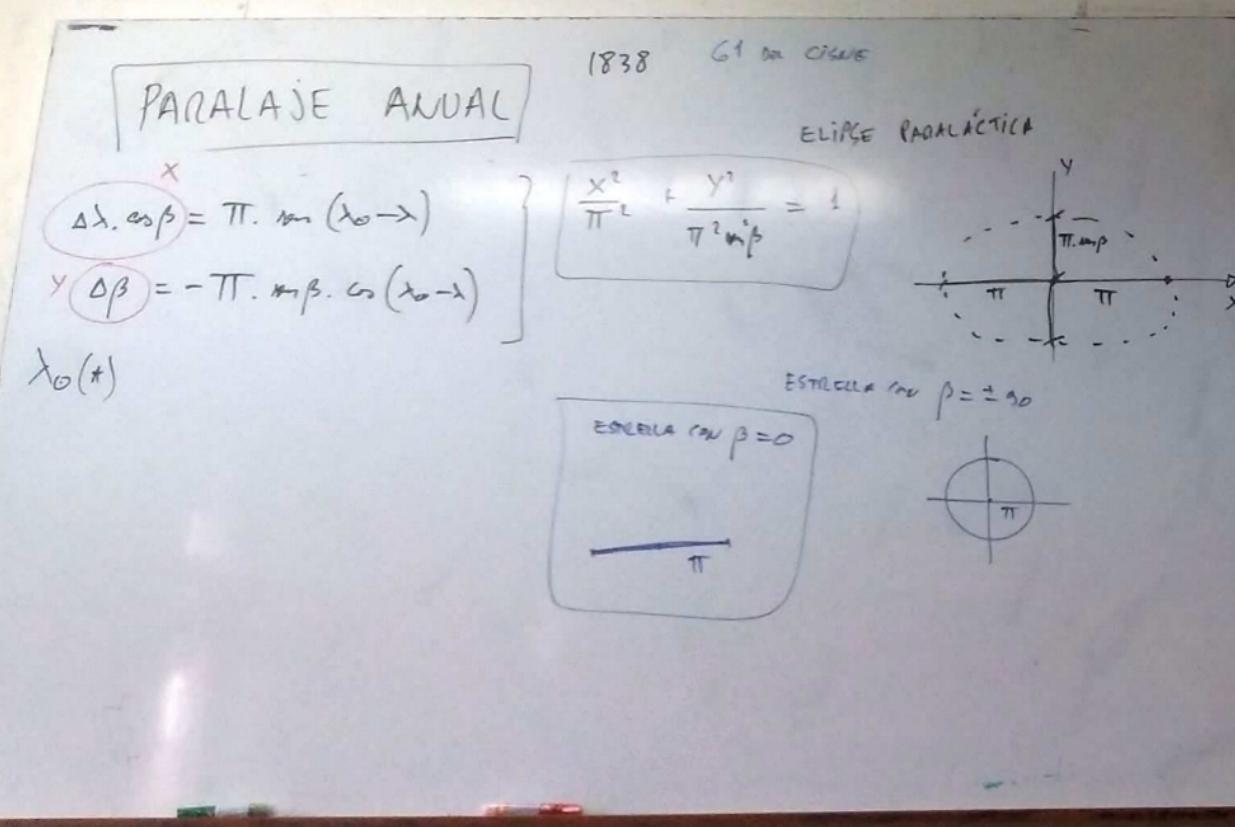
$$m\theta \cdot (-m\psi) = -m\beta \cdot \cos(\lambda_0 - \lambda)$$

$$m\theta \cdot m\psi = m\beta \cdot \cos(\lambda_0 - \lambda) \quad (2)$$

F. SENO

$$\frac{m(\lambda_0 - \lambda)}{m\theta} = \frac{m(\alpha + \psi)}{m\alpha} \xrightarrow{\text{cos}\psi} \Rightarrow m(\lambda_0 - \lambda) = m\theta \cdot \cos\psi \quad (1)$$





### PARALAJE ANUAL

$$\Delta\lambda \cdot \cos\beta = \pi \cdot m_p (\lambda_0 \rightarrow)$$

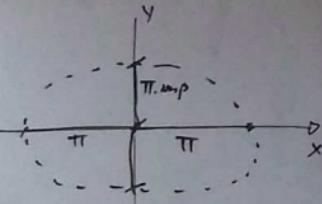
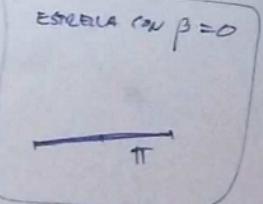
$$y \Delta\beta = -\pi \cdot m_p \beta \cdot \cos(\lambda_0 - \lambda)$$

$$\lambda_0(t)$$

1838 G1 de CISENE

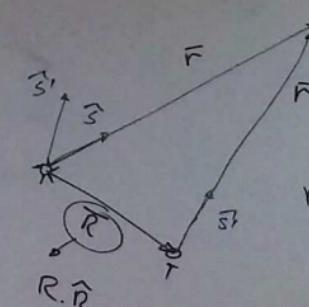
ELÍPSE PARALÁCTICA

$$\frac{x^2}{\pi^2} + \frac{y^2}{\pi^2 m_p^2} = 1$$

ESTRELLA CON  $\beta = \pm 90^\circ$ 

### FORMULACIÓN VECTORIAL

$$\vec{r} = \vec{R} + \vec{r}'$$



$$\vec{r}' \cdot \hat{s}' = \vec{r} \cdot \hat{s} - \vec{R} \cdot \hat{n}$$

$$\vec{r}' \cdot \hat{s} \wedge \hat{s}' = \vec{r} \cdot \hat{s} \wedge \hat{s} - \vec{R} \cdot \hat{s} \wedge \hat{n}$$

$$\vec{r}' \cdot \hat{s}_n (\hat{s} \wedge \hat{s}') = -\vec{R} \cdot \hat{s}_n (\hat{s} \wedge \hat{n})$$

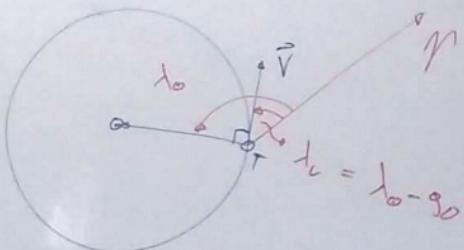
$$\vec{r}' \left[ (\hat{s} \cdot \hat{s}') \cdot \hat{s} - (\hat{s} \cdot \hat{s}) \cdot \hat{s}' \right] = -\vec{R} \left[ (\hat{s} \cdot \hat{n}) \cdot \hat{s} - (\hat{s} \cdot \hat{s}) \cdot \hat{n} \right]$$

$$\vec{r}' (\hat{s} - \hat{s}') = -\vec{R} ((\hat{s} \cdot \hat{n}) \cdot \hat{s} - \hat{n})$$

$$\overline{ds} = \left( \frac{\vec{R}}{\vec{r}'} \right) [(\hat{s} \cdot \hat{n}) \cdot \hat{s} - \hat{n}]$$

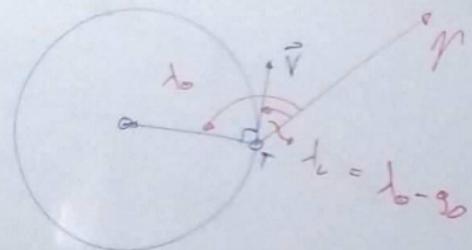
$$\overline{ds} = \hat{s}' - \hat{s}$$

ABERRACIÓN ANUAL



$$\Delta\theta = \frac{v}{c} \cdot \tan \theta$$

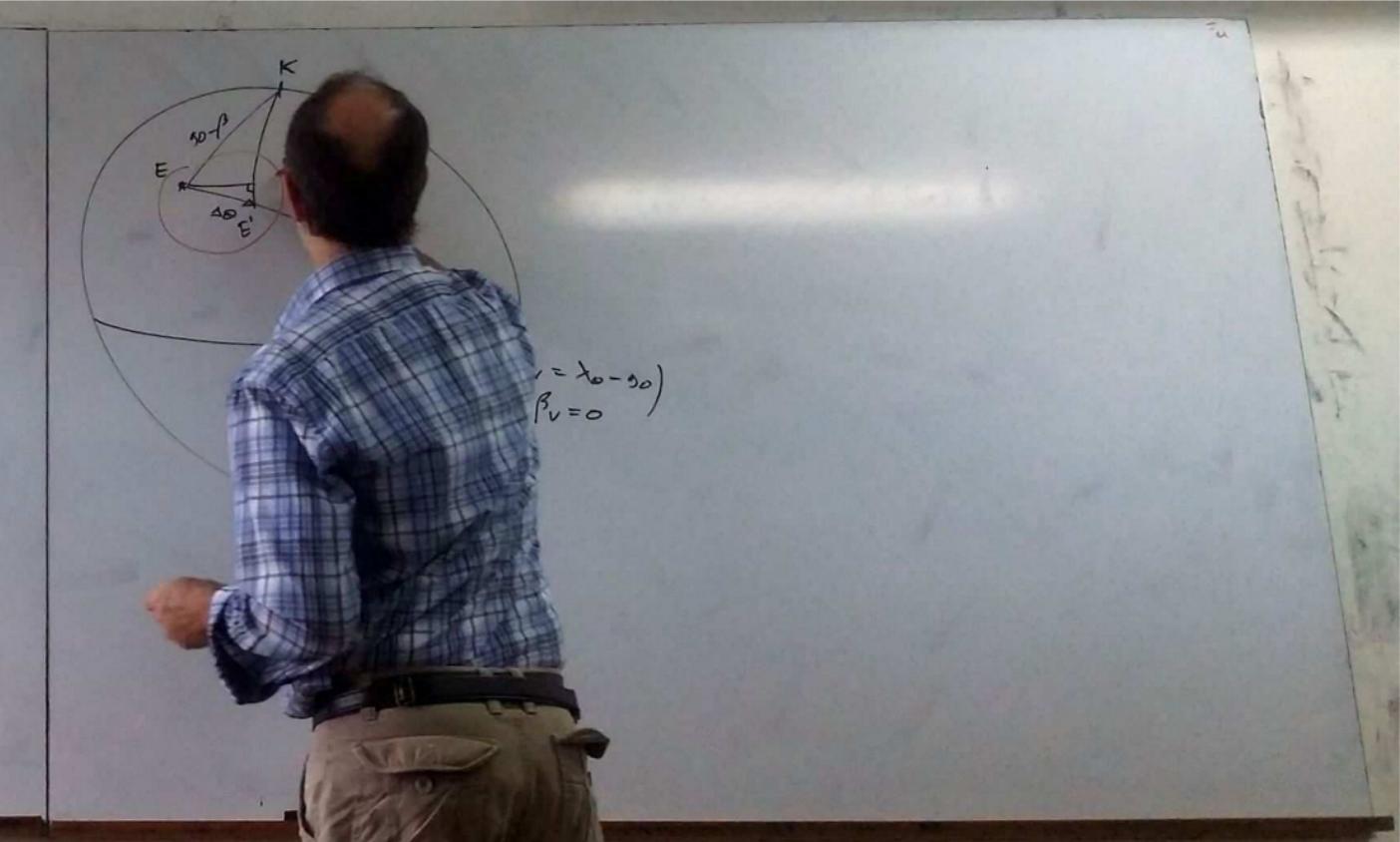


**ABERRACIÓN ANUAL**

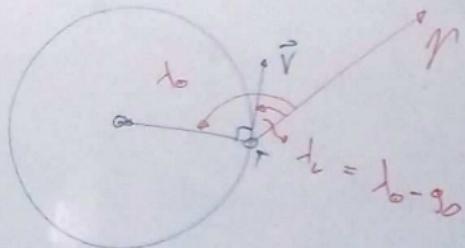
$$\Delta\theta = \frac{V}{c} \cdot \theta$$

30 Km/s

A diagram showing a star at the top with a velocity vector  $\vec{v}$  pointing down and to the left. A vector  $\vec{n}$  points from the star towards the bottom-left. A small angle  $\alpha$  is shown between the vertical line and the vector from the star to the point of observation. A vector  $\vec{r}$  points from the star to the point of observation, making an angle  $\beta$  with the vertical line. The angle between  $\vec{r}$  and  $\vec{v}$  is labeled  $\Delta\theta$ .

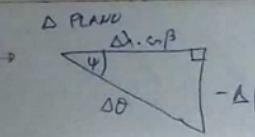
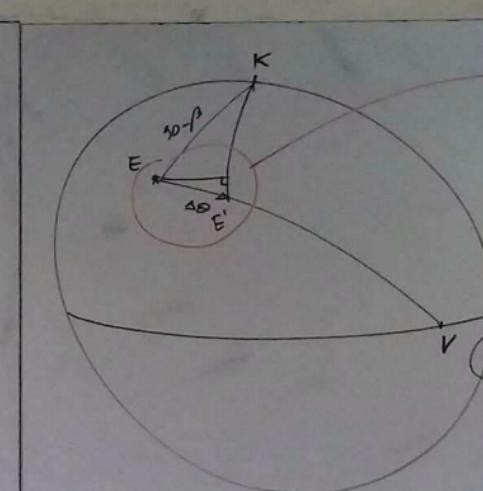


### ABERRACIÓN ANUAL



$$\Delta\theta = \frac{v}{c} \cdot \sin\theta$$

30 km/s

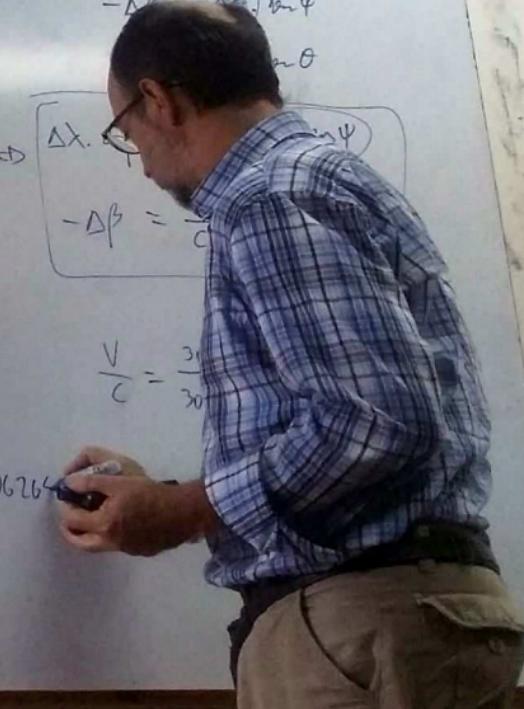


$$\Rightarrow \Delta x \cdot \sin\beta = \Delta\theta \cdot \sin\Psi$$

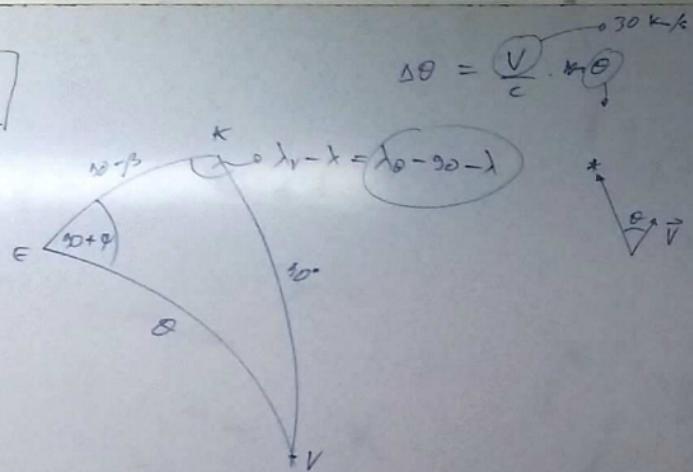
$-\Delta\beta = \frac{\Delta\theta \cdot \sin\Psi}{\sin\theta}$

$$\frac{v}{c} = \frac{30}{30}$$

$$1_{\text{rad}} = 206264$$

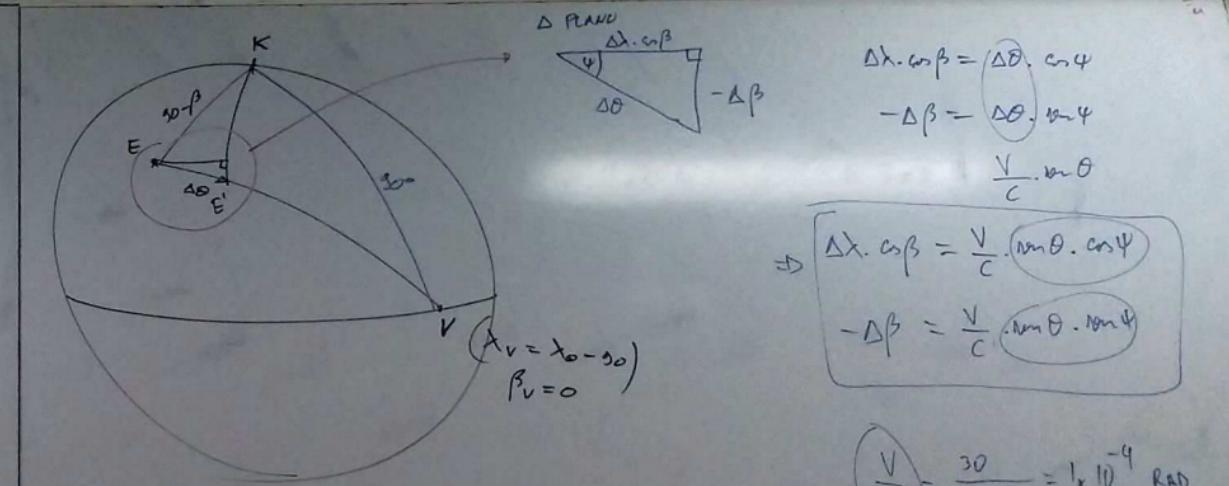


### ABERRACIÓN ANUAL



$$\Delta\theta = \frac{v}{c} \cdot \sin \theta$$

$$\lambda_V - \lambda = \lambda_0 - \delta_0 - \lambda$$



$$\Delta \text{PLANO} = \Delta\theta \cdot \cos \beta$$

$$\Delta\lambda \cdot \cos \beta = \Delta\theta \cdot \cos \psi$$

$$-\Delta\beta = \Delta\theta \cdot \tan \psi$$

$$\frac{v}{c} \cdot \sin \theta$$

$$\Rightarrow \Delta\lambda \cdot \cos \beta = \frac{v}{c} \cdot \sin \theta \cdot \cos \psi$$

$$-\Delta\beta = \frac{v}{c} \cdot \sin \theta \cdot \tan \psi$$

$$\frac{v}{c} = \frac{30}{300.000} = 1 \cdot 10^{-4} \text{ RAD}$$

$$1 \text{ RAD} = 206265''$$

$$10^{-4} \text{ RAD} > 20.6$$

$$20.6'' = K$$

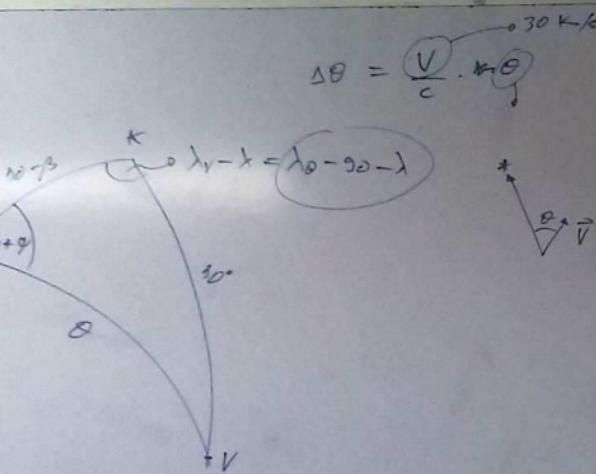
CTE  
ABERRACIÓN

### ABERRACIÓN ANUAL

$$\Rightarrow (\Delta\lambda \cdot \cos\beta) = -K \cdot \cos(\lambda_0 - \lambda)$$

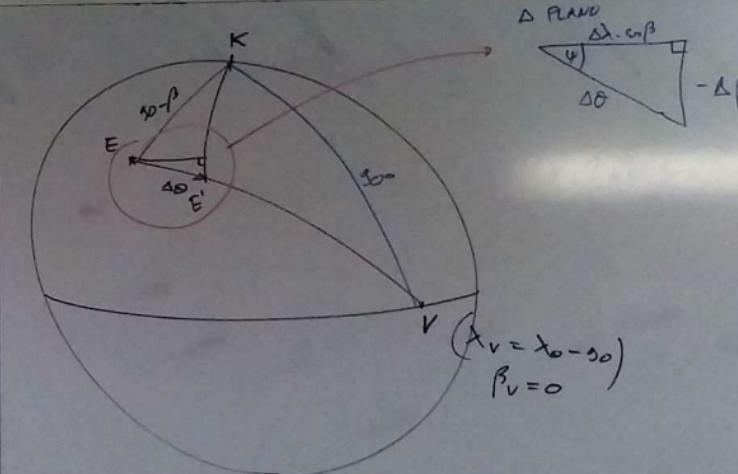
$$(\Delta\beta) = -K \cdot \sin\beta \cdot \sin(\lambda_0 - \lambda)$$

$$\frac{x^2}{K^2} +$$



$$\Delta\phi = \frac{v}{c} \cdot \sin\theta$$

$$\lambda_v - \lambda = \lambda_0 - \lambda_0 - \lambda$$



$$\Delta\lambda \cdot \cos\beta = \Delta\phi \cdot \cos\psi$$

$$-\Delta\beta = \Delta\phi \cdot \sin\psi$$

$$\frac{v}{c} \cdot \sin\theta$$

$$\Delta\lambda \cdot \cos\beta = \frac{v}{c} \cdot \sin\theta \cdot \cos\psi$$

$$-\Delta\beta = \frac{v}{c} \cdot \sin\theta \cdot \sin\psi$$

$$\left( \frac{v}{c} \right) = \frac{30}{300.000} = 1 \cdot 10^{-4} \text{ RAD}$$

$$1 \text{ RAD} = 206265''$$

$$(10^{-4} \text{ RAD}) = 20.6$$

$$20.6 = K$$

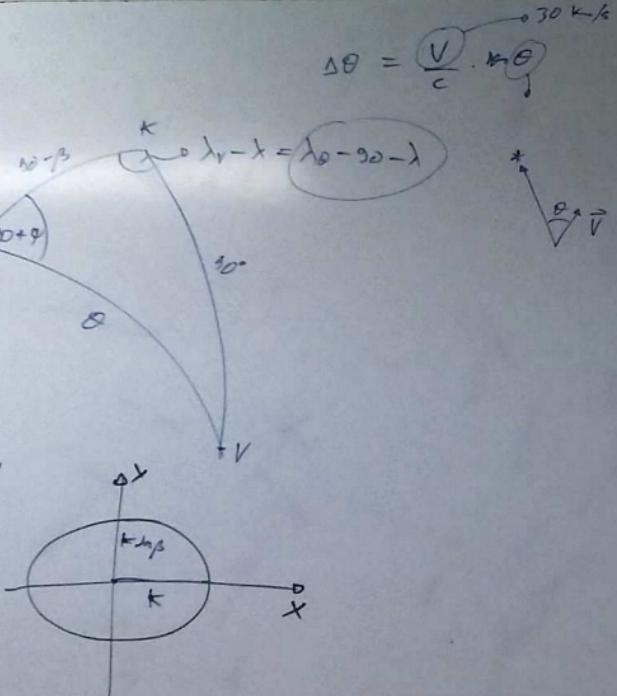
CTE  
ABERRACIÓN

### ABERRACIÓN ANUAL

$$\Rightarrow (\Delta\lambda \cdot \cos\beta) = -K \cdot \cos(\lambda_0 - \lambda)$$

$$(\Delta\beta) = -K \cdot \sin\beta \cdot \sin(\lambda_0 - \lambda)$$

$$\frac{x^2}{K^2} + \frac{y^2}{K^2 m_p^3} = 1$$

ELÍPSE DE  
ABERRACIÓN

$$\Delta\theta = \frac{V}{c} \cdot m\theta$$

$$\lambda_r - \lambda = \lambda_0 - \lambda_0 - \lambda$$

$$\Delta\lambda \cdot \cos\beta = \Delta\theta \cdot \cos\beta$$

$$-\Delta\beta = \Delta\theta \cdot \sin\beta$$

$$\frac{V}{c} \cdot m\theta$$

$$\Rightarrow \Delta\lambda \cdot \cos\beta = \frac{V}{c} \cdot m\theta \cdot \cos\beta$$

$$-\Delta\beta = \frac{V}{c} \cdot m\theta \cdot \sin\beta$$

$$\left(\frac{V}{c}\right) = \frac{30}{300.000} = 1 \cdot 10^{-4} \text{ RAD}$$

$$1 \text{ RAD} = 206265''$$

$$10^{-4} \text{ RAD} > 20.6$$

$$20.4 = K$$

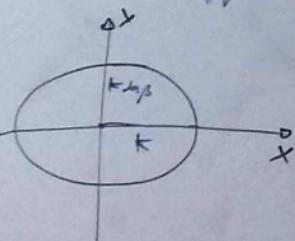
CTE DE  
ABERRACIÓN

### ABERRACIÓN ANUAL

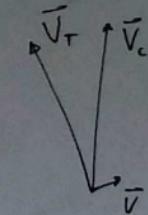
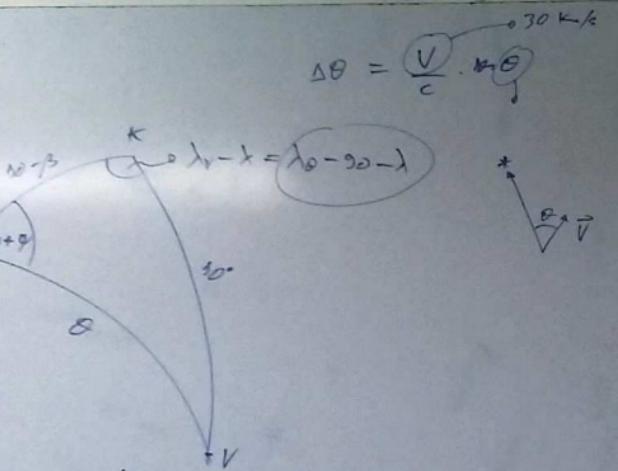
$$\Delta\lambda \cdot \cos\beta = -K \cdot \cos(\lambda_0 - \lambda)$$

$$\Delta\beta = -K \cdot \sin\beta \cdot \sin(\lambda_0 - \lambda)$$

$$\frac{x^2}{K^2} + \frac{y^2}{K^2 M_p^2} = 1$$

ELÍPSE DE  
ABERRACIÓN

$$\Delta\theta = \frac{V}{c} \cdot \sin\theta$$



$$\Delta\lambda \cdot \cos\beta = \Delta\theta \cdot \cos\psi$$

$$-\Delta\beta = \Delta\theta \cdot \sin\psi$$

$$\frac{V}{c} \cdot \sin\theta$$

$$\Delta\lambda \cdot \cos\beta = \frac{V}{c} \cdot \sin\theta \cdot \cos\psi$$

$$-\Delta\beta = \frac{V}{c} \cdot \sin\theta \cdot \sin\psi$$

$$\frac{V}{c} = \frac{30}{300.000} = 1 \cdot 10^{-4} \text{ RAD}$$

$$1 \text{ RAD} = 206265''$$

$$10^{-4} \text{ RAD} = 20.6$$

$$20.6 = K$$

CTE DE  
ABERRACIÓN

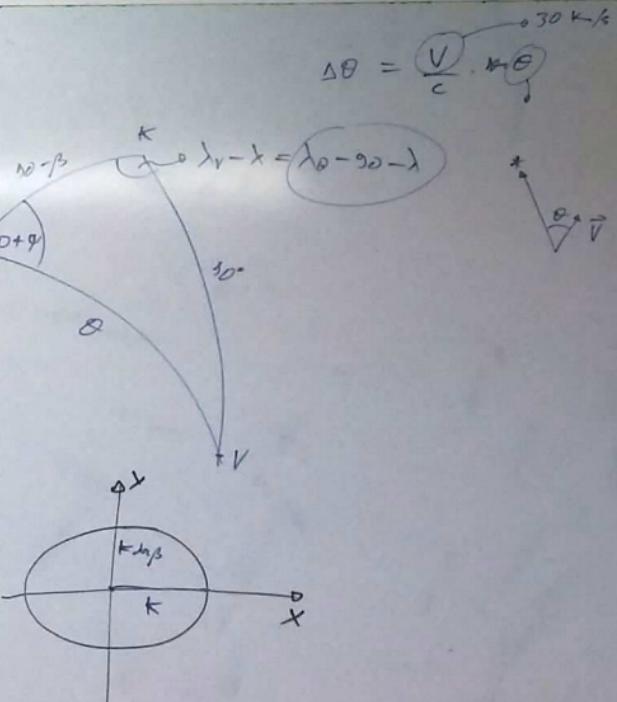
### ABERRACIÓN ANUAL

$$\Delta\lambda_{\alpha\beta} = -K \cdot \cos(\lambda_0 - \lambda)$$

$$\Delta\beta = -K \cdot \sin\beta \cdot \sin(\lambda_0 - \lambda)$$

$$\frac{x^2}{K^2} + \frac{y^2}{K^2 \sin^2\beta} = 1$$

ECLIPSE DE  
ABERRACIÓN



$$\Delta\lambda_{\alpha\beta}$$



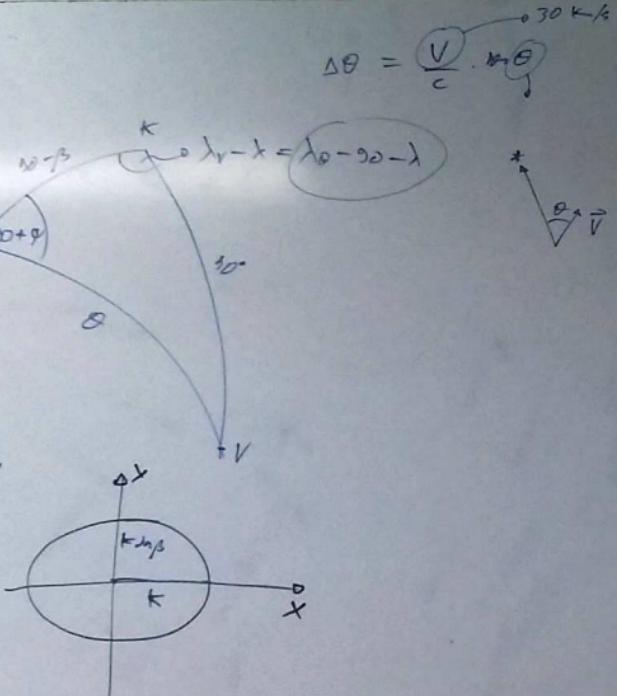
### ABERRACIÓN ANUAL

$$\Rightarrow (\Delta\lambda, \alpha\beta) = -K \cdot \cos(\lambda_0 - \lambda)$$

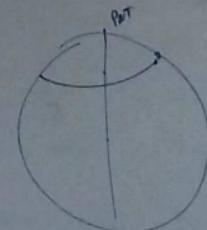
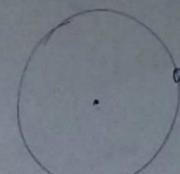
$$(\Delta\beta) = -K \cdot \sin\beta \cdot \sin(\lambda_0 - \lambda)$$

$$\frac{x^2}{K^2} + \frac{y^2}{K^2 M_p^3} = 1$$

EJERCICIO  
ABERRACIÓN



$$y = \frac{P}{r} \left( \sin\alpha \cos\phi' \sin\theta - \sin\alpha \sin\phi' \right)$$



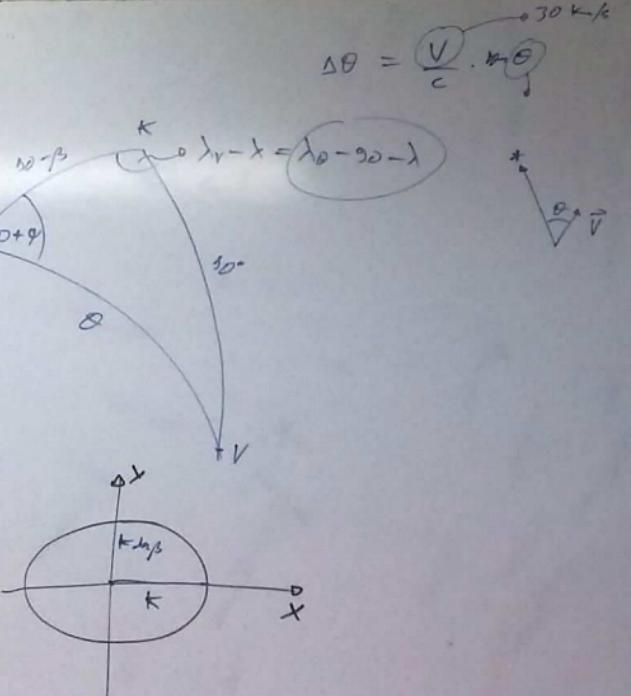
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$$\Rightarrow (\Delta\lambda, \Delta\beta) = -K \cdot \cos(\lambda_0 - \lambda)$$

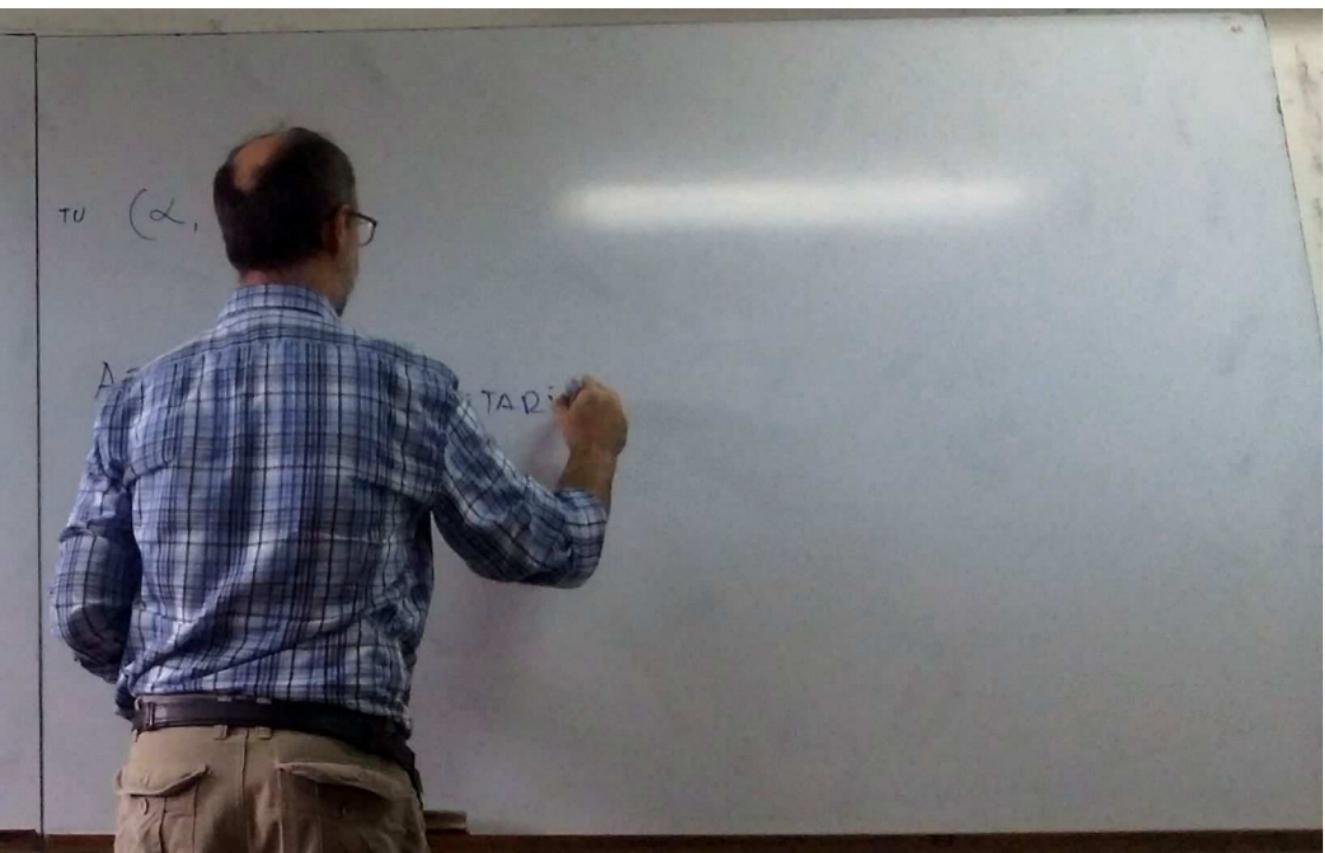
$$(\Delta\beta) = -K \cdot v \sin \beta \cdot \sin(\lambda_0 - \lambda)$$

$$\frac{x^2}{K^2} + \frac{y^2}{K^2 v \sin^2 \beta} = 1$$

ECLIPSE DE  
ABERRACIÓN



$$\Delta\theta = \frac{V}{c} \cdot \frac{K}{r}$$



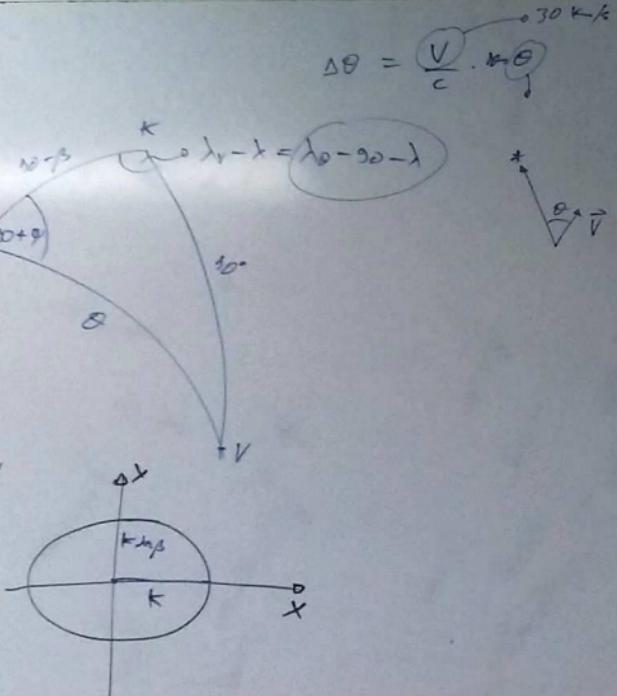
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ELÍPSE DE  
ABERRACIÓN



TU  $(\alpha, \delta)$   $\rightarrow$  DIST OBJETO - TIERRA =  $\zeta$

ABERRACIÓN PLANETARIA = CORRECCIÓN POR TIEMPO-LUZ

$$\lambda_{obs} = \lambda - \zeta \cdot \frac{dd}{dx}$$

$$\delta_{obs} = \delta - \zeta \cdot \frac{df}{dt}$$